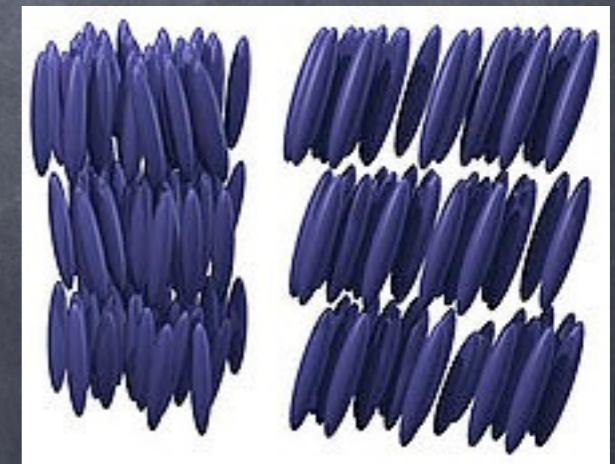


Discussion of Electronic Nematic State

SHI Hongjie

Introduction: What is Nematic phase

- The word “Nematic” originally comes from Liquid Crystal (LCs 液晶).
- Liquid crystal is the a state of matter that have properties between those of conventional liquid and a solid crystal.
- Within a nematic phase, rod-shaped molecule have no position order, but they self align to have long-range directional order. (LCD)
- A smectic phase happens below temperature of nematic phase, by forming well-defined layer. Smectics are positional ordered in one direction.



Analogy: What is Electronic Nematic phase

- With weak interaction, electron can be considered as quantum gas of quasiparticle -- fermi-liquid, homogeneous and isotropic. Analog to liquid.
- Sufficient strong interaction, electrons crystallize, freezing into an insulating state, exhibits density modulations. Analog to crystals.
- View from symmetry-breaking
- **Definition:**
 - (1) Liquid phase breaks no spatial symmetry.
 - (2) Nematic phase breaks rotation symmetry, but leaves both translation and reflection symmetry unbroken.
 - (3) Smectic phase breaks translation symmetry in only one direction.
 - (4) Crystalline phase breaks translation symmetry.

Define Electronic Nematic phase order parameter

$$\mathcal{N} = \frac{\rho_{xx} - \rho_{yy}}{\rho_{xx} + \rho_{yy}}$$

$$Q_{\mathbf{k}} \equiv \frac{S(\mathbf{k}) - S(\mathcal{R}[\mathbf{k}])}{S(\mathbf{k}) + S(\mathcal{R}[\mathbf{k}])},$$

where \mathcal{R} is rotation by $\pi/2$, and

$$S(\mathbf{k}) = \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} S(\mathbf{k}, \omega)$$

$$\mathcal{N} = \frac{\langle \vec{\sigma}_{\vec{R}} \cdot \vec{\sigma}_{\vec{R}+\hat{x}} \rangle - \langle \vec{\sigma}_{\vec{R}} \cdot \vec{\sigma}_{\vec{R}+\hat{y}} \rangle}{\langle \vec{\sigma}_{\vec{R}} \cdot \vec{\sigma}_{\vec{R}+\hat{x}} \rangle + \langle \vec{\sigma}_{\vec{R}} \cdot \vec{\sigma}_{\vec{R}+\hat{y}} \rangle}$$

etc...

Mechanism of Electronic Nematic

- Analog to liquid crystal: How point-like shapeless electron behaves stripe-like nematic order.

Mechanism of Electronic Nematic: Two perspectives

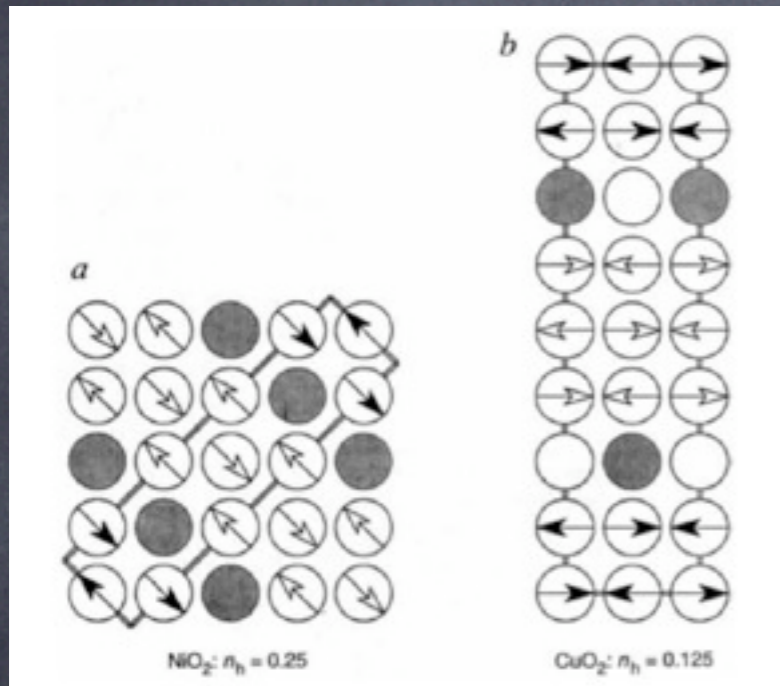
- Strong correlated system: nematic state derives from melting of smectic state.
- Fermi-liquid-like perspective: Pomeranchuk instability breaks symmetry of fermi surface defined by quasiparticles.

Mechanism — — A melting process: what is electronic stripe order

- **CONDITION** Coulomb interactions are sufficiently weak (dielectric constant is large enough)
RESULT System lower its energy by locally phase separating into small regions of hole-rich and hole-poor material (charge density inhomogeneous)
- Considering quantum dynamical process, heavily-doped material: creating small dipolar regions does NOT involve large motion of charge.
Local, low-energy collective modes: Classical dipolar becomes Local dipolar modes. (measured by antiferromagnetic correlation length etc.)

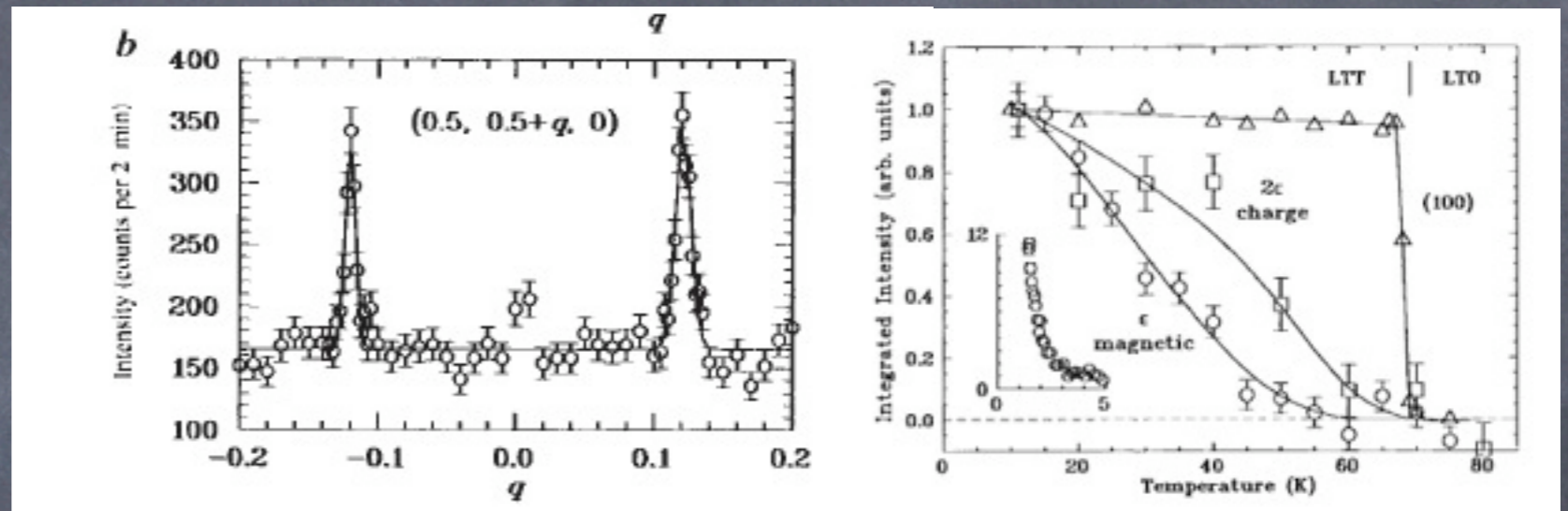
Electronic stripe order

Experiment evidence: High Tc cuprate SC



a, Idealized diagram of spin and charge stripe pattern in NiO_2 plane

b, Hypothesized stripe pattern in CuO_2 plane of La_2CuO_4



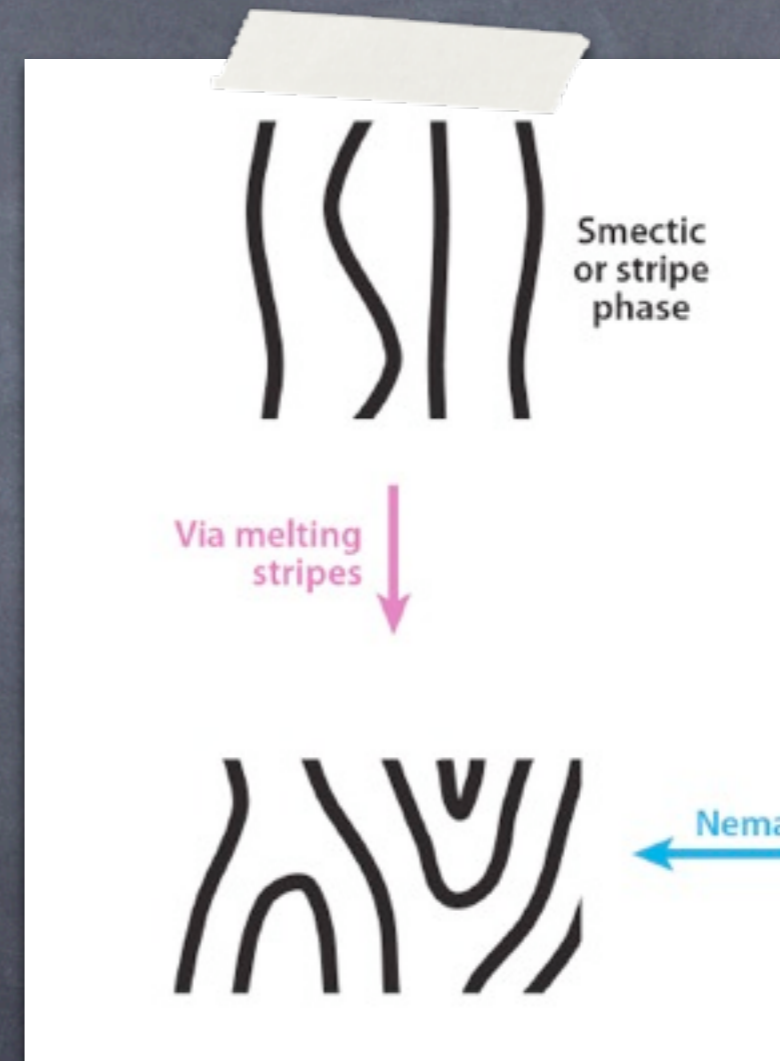
LEFT: Scans of superlattice peaks incommensurate with the crystal lattice, HOWEVER consistent with the proposed spin and charge stripes. $\text{La}_{1.48}\text{Nd}_{0.4}\text{Sr}_{0.12}\text{CuO}_4$ at 11 K.

RIGHT: Temperature dependence of peak intensities. Results show for the magnetic $(0.5, 0.5-\epsilon, 0)$ (circle), charge-related $(0, 2-2\epsilon, 0)$ (squares).

Mechanism of Electronic Nematic

Outline: a melting process

- Similar to the theory developed in complex classical fluids.
- Keyword: dislocations — — topological defects of strips
- Take place via thermal phase transition or quantum phase transition.



Mechanism — — melting process : A simple model of 2-D stripe array

Consider an isolated metallic stripe in a Mott insulator

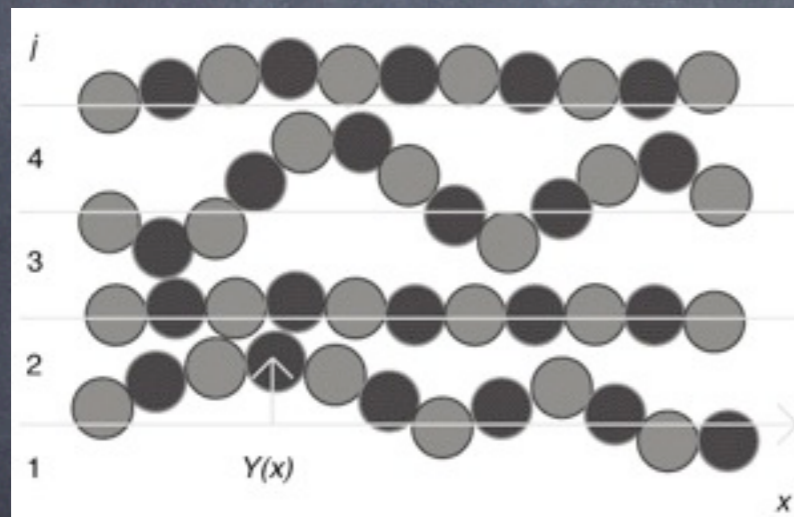


Figure: Schematic representation of a smectic stripe phase. The circles represent periodic structures along the stripes, which are forced out of phase by the transverse fluctuations.

Interactions between stripes typically drive a transition to an insulating ordered charge-density-wave (CDW) state at low temperature.

$$H_c = \sum_j \int dx V(\Delta_j, Y) \cos[\sqrt{2\pi}(\Delta_j \phi) - 2k_F(\Delta_j L)] \quad (4)$$

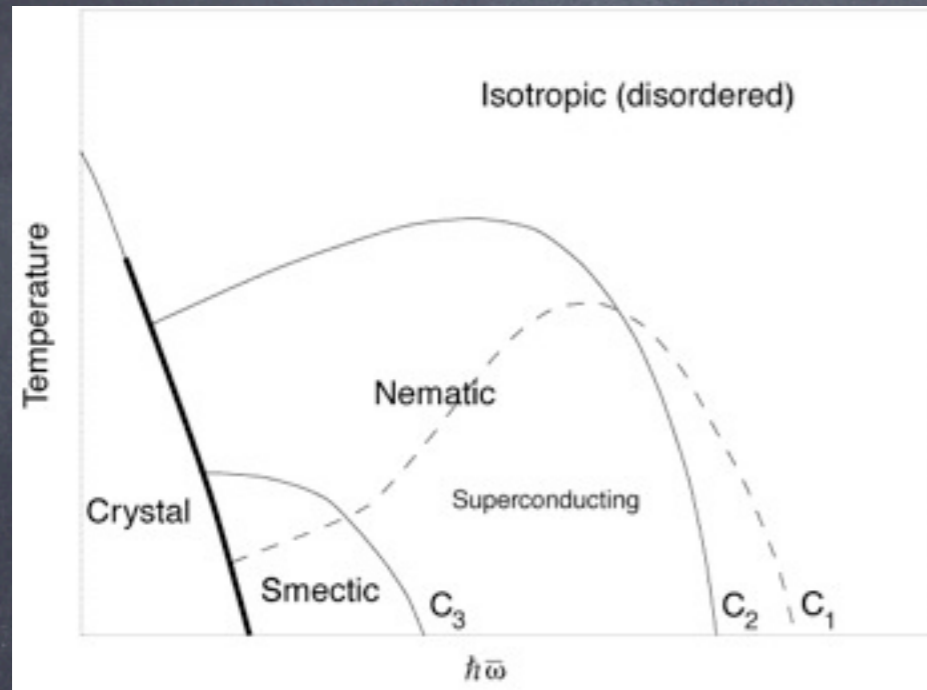
The coupling Hamiltonian between the CDWs on neighboring stripes

“ ϕ ” defines the phase of the CDW

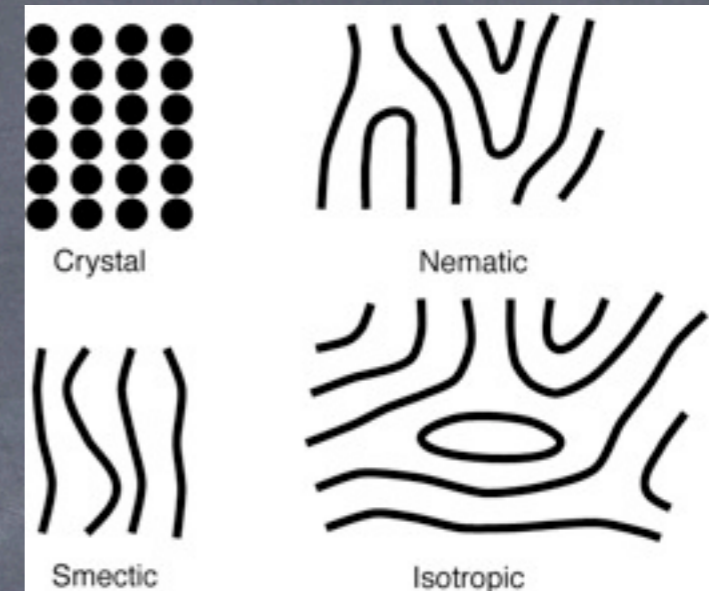
“ L ” is the arc-length, that is the distance measured along the stripe j .

Mechanism — — melting process

A simple model of 2-D stripe array: Results discussion



Phase diagram: Here “ $h\bar{\omega}$ ” is a measure of magnitude of transverse zero-point fluctuations of the stripes



- Low “ $h\bar{\omega}$ ” the phases of CDWs on neighboring strips are locked, the transverse stripe fluctuations become the phonons of fully ordered crystal.

$$\langle J \rangle \approx J_0 \exp\{(\alpha^2/2)\langle[\Delta_j Y]^2\rangle\} \quad (8)$$

Effective Josphenson Coupling.
Hence the superconducting coupling is strongly enhanced by the transverse stripe fluctuations.

Mechanism — — A melting process: General consideration

- The theory of quantum smectic-nematic phase transition by a dislocation proliferation mechanism remains an open problem.
- Since the degrees of freedoms are electrons, from which these nano-structures form, electron nematic is typically an anisotropic metal.
- Similarly, nematic order can also arise from thermal or quantum melting a frustrated quantum antiferromagnet.

Mechanism — — Pomeranchuk instability: Fermi-liquid-like perspective

- Classic result due to Pomeranchuk (1958), that shows a Fermi liquid is thermodynamically stable. However if some conditions are violated a thermodynamic (Pomeranchuk) instability occurs.
- Along with Pomeranchuk instability, the system must undergo a quantum phase transition in which the symmetries of the Fermi liquid state are lowered.
- The anisotropic nature of nematic ground state leads to a transport anisotropy, which is tuned by magnitude of the order parameter.
- No suitable quantitative theory for these problems yet. Hartree-Fock theory is not reliable in strong correlation regimes. There are conflicting results on some subjects.

How to detect Electronic Nematic Order or Fluctuation

- difficulty and ambiguousness

How to detect Electronic Nematic Order/Fluctuation Strategies

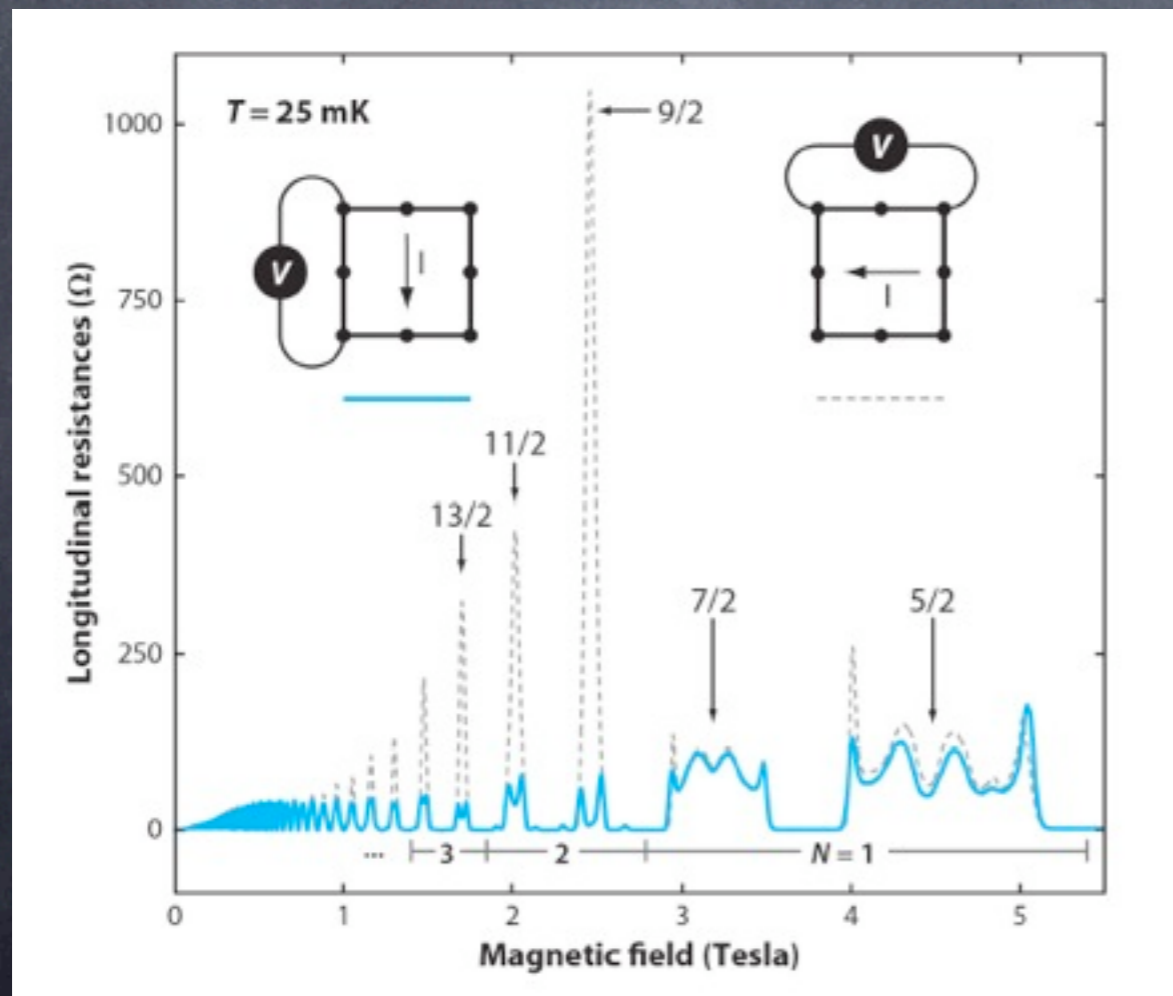
- Generally, we are interested in electronic liquid-crystal states and their associated fluctuations, but the results are also easily generalized to other forms of order.
- Although nematic order involves the spontaneous breaking of a spatial symmetry, true macroscopic measurements of spontaneous nematic symmetry breaking are not possible.
- The ordered phase may be induced by making small changes to the chemical composition of material, applying pressure or magnetic fields, etc.
- Almost all tests of nematic order necessarily involve the observation of an unreasonably large, and strongly T-dependent, anisotropy in electronic response to a small symmetry-breaking field.

How to detect Electronic Nematic Order/Fluctuation Strategies

- Typically, the best way to detect both the broken-symmetry state and the relevant fluctuations is by appropriate dynamical structure factor $S(q,\omega)$.
- Indeed x-ray and neutron scattering studies have provided the best evidence of ordered and fluctuating stripe phases.
- However, in many interesting materials, appropriate crystals are not available. Here, probes of local order, such as NMR, NQR, μ SR, STM techniques may be the best available.
- In a pure quantum system, the order-parameter fluctuations are not static. Unless something is done to pin these fluctuation, they are invisible to local probes.
- Pinning such as boundaries, vortices, crystal-field effects, weak quenched disorder , etc.

GaAs/GaAlAs Experiment facts: Evidence of existence of electronic nematic phase

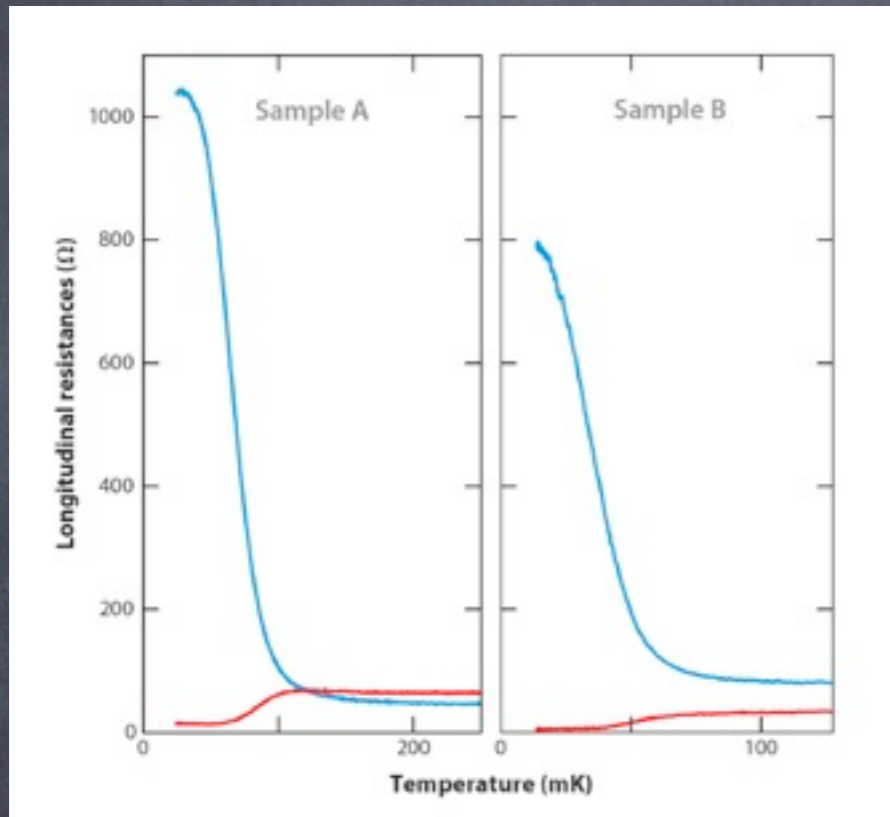
- Two-dimensional electron systems.
- Best known for their display of fractional quantized Hall (FQH) effect, when a large magnetic field is applied perpendicularly.



Substantial resistance anisotropy was observed by a perpendicular magnetic field to 2-D plane.

At Landau level filling factor $\nu=9/2$, 11/2, 13/2 etc. T=25mK

GaAs/GaAlAs Experiment facts: Evidence of existence of electronic nematic phase

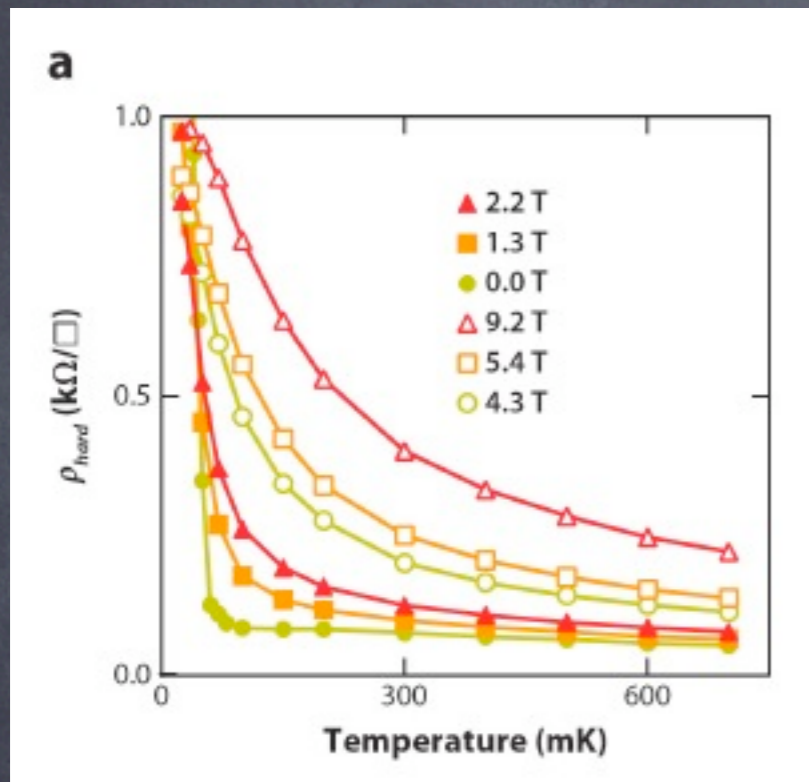


- The anisotropy subsides rapidly with increasing T , and is essentially absent above $T=150\text{mK}$
- This effect is largely independent of temperature and magnetic field.
- Hard transport direction lies along $\langle 1\bar{1}0 \rangle$, stripes tend to lie along $\langle 110 \rangle$.
- In-plane field along $\langle 110 \rangle$ interchange hard and easy transport direction.

GaAs/GaAlAs Experiment facts: Evidence of existence of electronic nematic phase

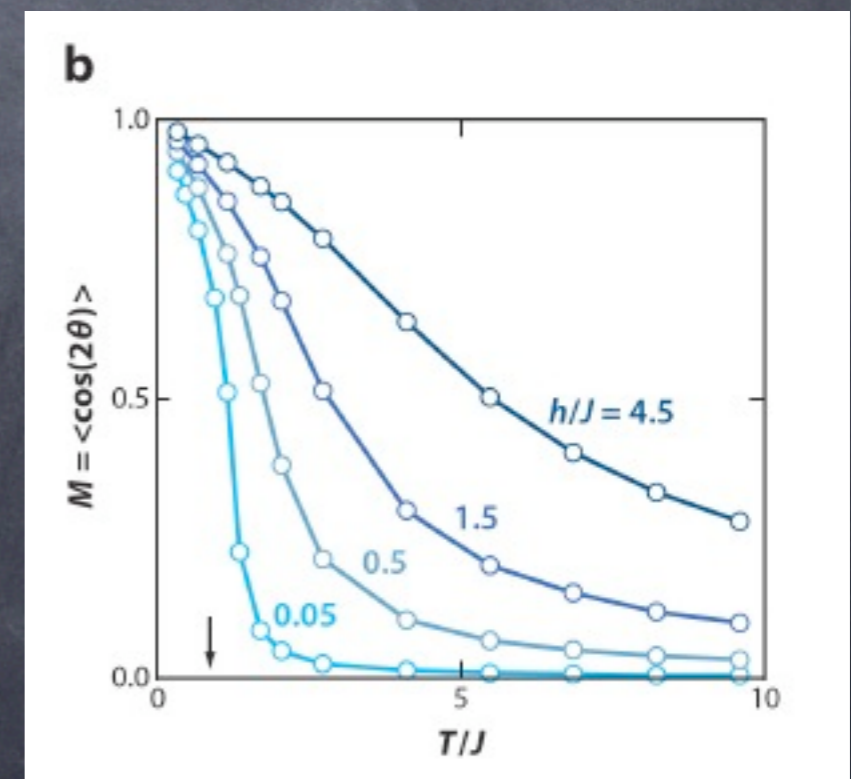
- Hartree-Fock theories of CDW formation estimated that CDWs would form at temperature is few Kelvin.
- Interesting possibility is that local stripe order may appear within small domains. Thermal fluctuations prevent long range orientational order.
- In this view, a in-plane magnetic field would order domains and thereby induce resistive anisotropy at elevated temperature.

GaAs/GaAlAs Experiment facts: Evidence of existence of electronic nematic phase

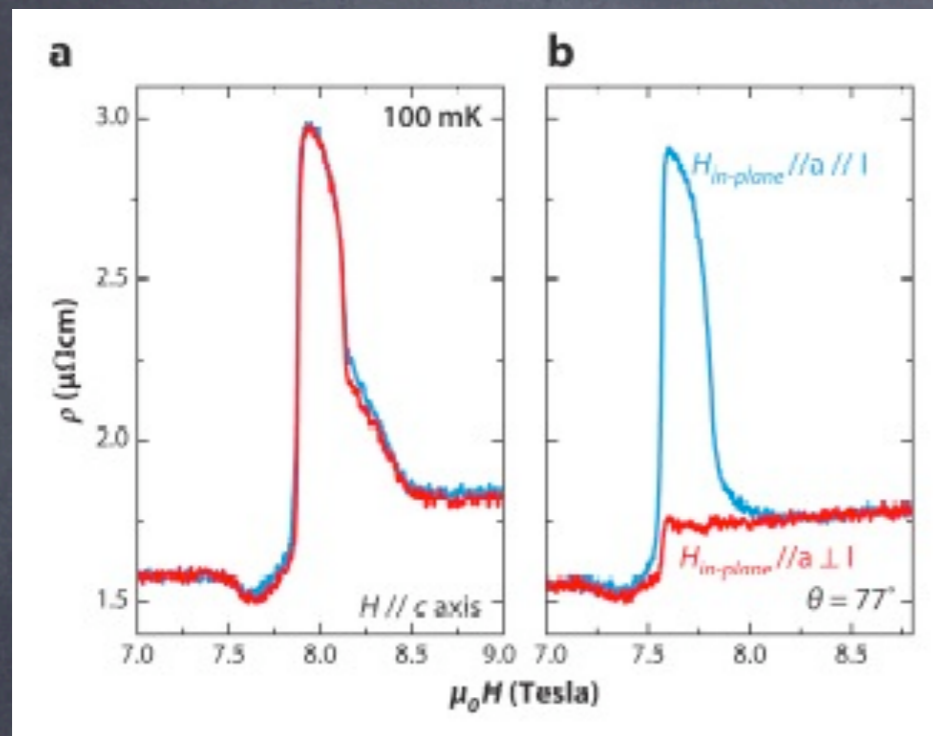


- In-plane field dramatically increases the temperature range of resistive anisotropy
- Importantly, no significant anisotropy at $\nu=3/2$, which discounts that in-plane field itself creating an anisotropy.

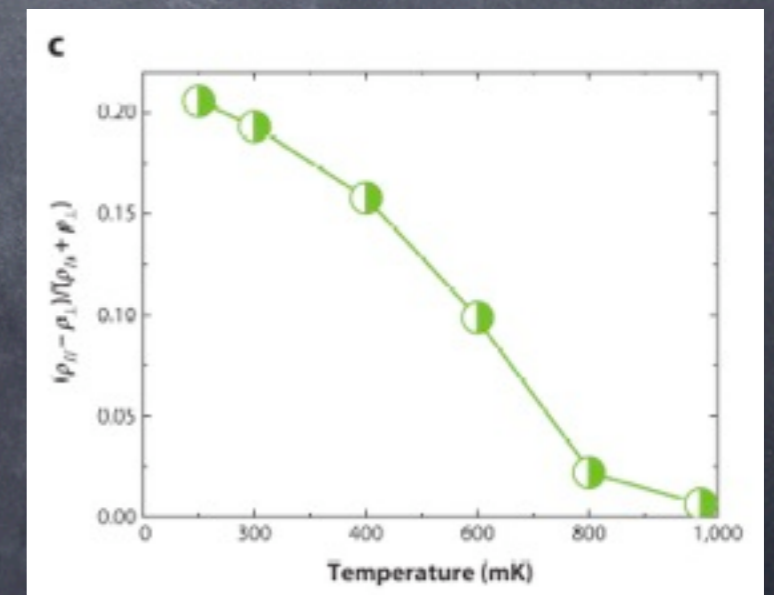
- reminiscent of how a ferromagnet responds to an external magnetic field.
- Results of Monte Carlo calculation on a 2D XY model with varying symmetry breaking potential.



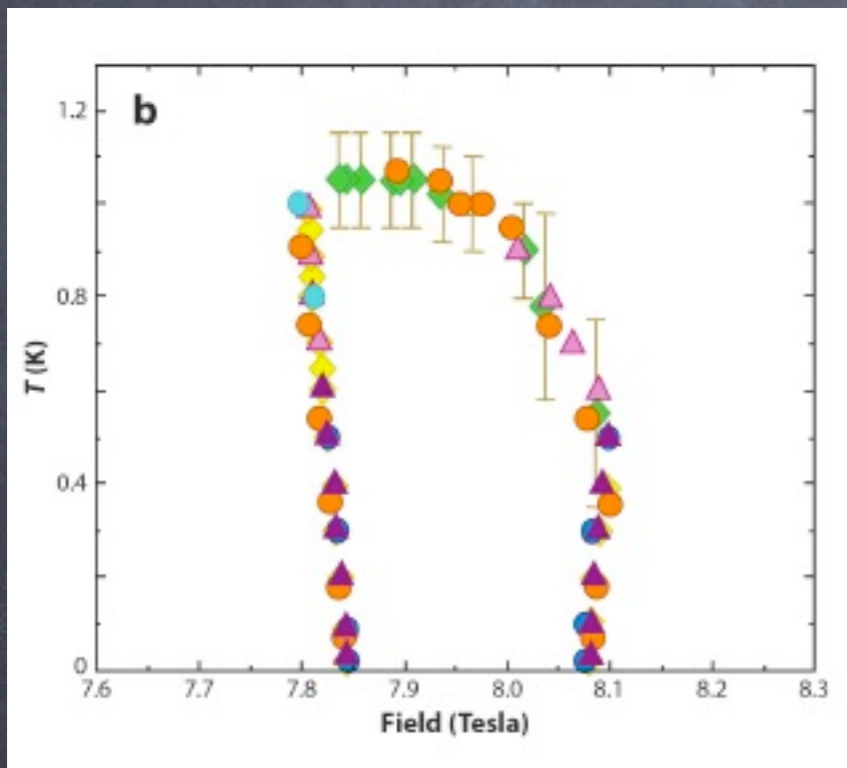
Bilayer ruthenate $\text{Sr}_3\text{Ru}_2\text{O}_7$ Experiment facts: Metamagnetism and Nematicity



- Applied by magnetic field along c-axis (perpendicular to conduction layer), it displays a standard metallic magnetoresistance.
 - However, if sample is tilted slightly to provide an in-plane field component, resistivity becomes strongly anisotropic.
- $\text{Sr}_3\text{Ru}_2\text{O}_7$ hosts a symmetry broken nematic phase between 7.8T and 8.1T. With domain formation masking the anisotropy.
 - Providing an in-plane field component aligns these domains and reveals full effects of symmetric breaking.



Bilayer ruthenate $\text{Sr}_3\text{Ru}_2\text{O}_7$ Experiment facts: Metamagnetism and Nematicity

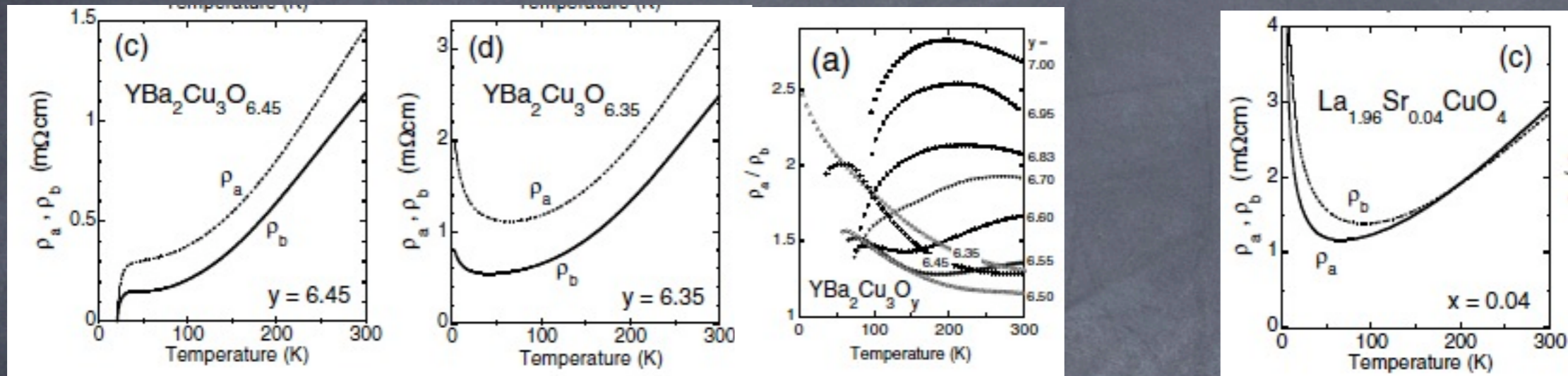


- Existence of a fully bounded thermodynamic phase.
- Magnetocaloric and specific heat show the boundary represent thermodynamic phase transition
- Within the resolution of neutron scattering, it is isotropic in the plane.
- Unusually, the entropy within the phase is higher than adjacent fluids.
- Open questions like: Entropy and scale of resistive anisotropy.

Cuprate high T_c superconductors experiment facts: Transport anisotropies

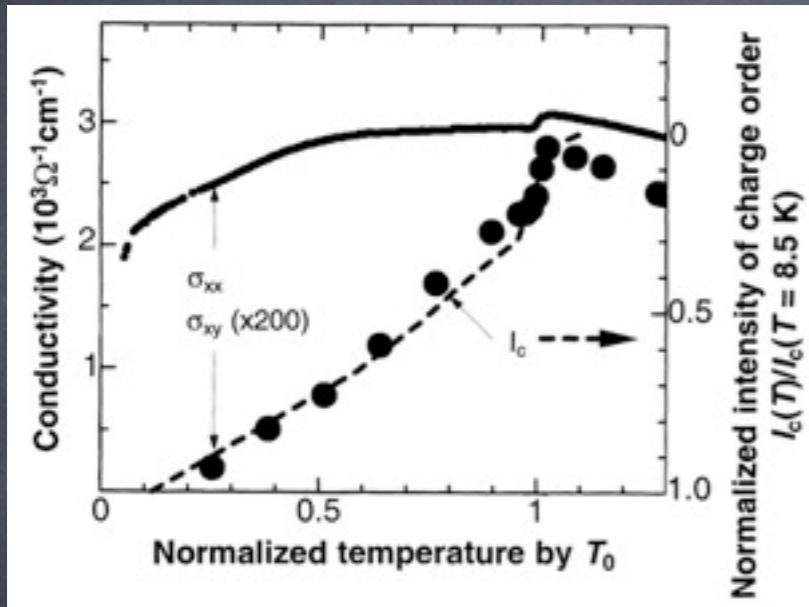
- Ex. $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$, $\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$ (non-sc), are orthorhombic.
Good: orthorhombicity exerts a symmetry breaking field.
Bad: macroscopic anisotropy is to be expected as a consequence of orthorhombicity itself.
- Same logic as before,
small and weakly T dependent anisotropies at High $T \rightarrow$ consequence of crystal structure.
Large magnitude, strongly T depend below a well defined crossover $T \rightarrow$ associated with onset of electronic nematic order.
- However, it is hard to say how large an observed anisotropy must be in order to accepted as “large” response to orthorhombicity, without a quantitative theory.

Cuprate high T_c superconductors experiment facts: Transport anisotropies



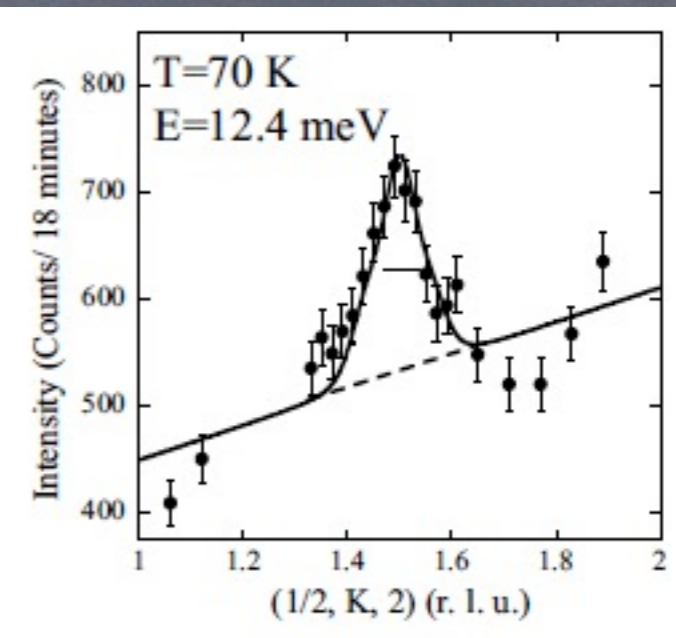
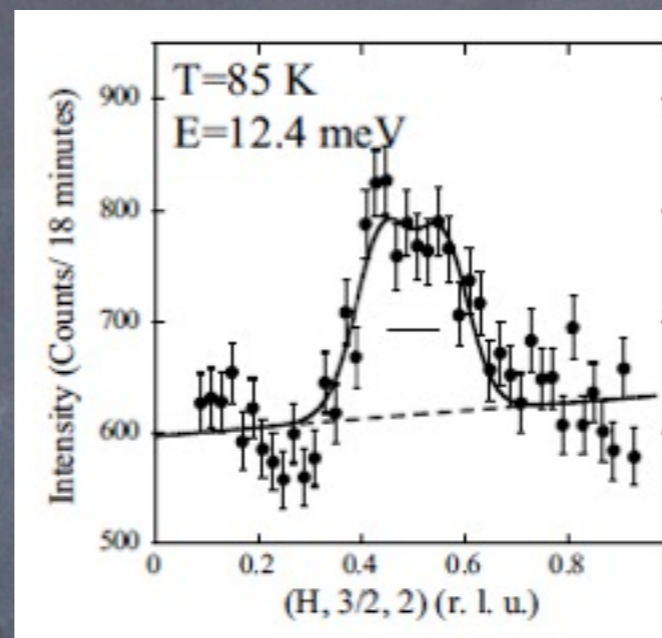
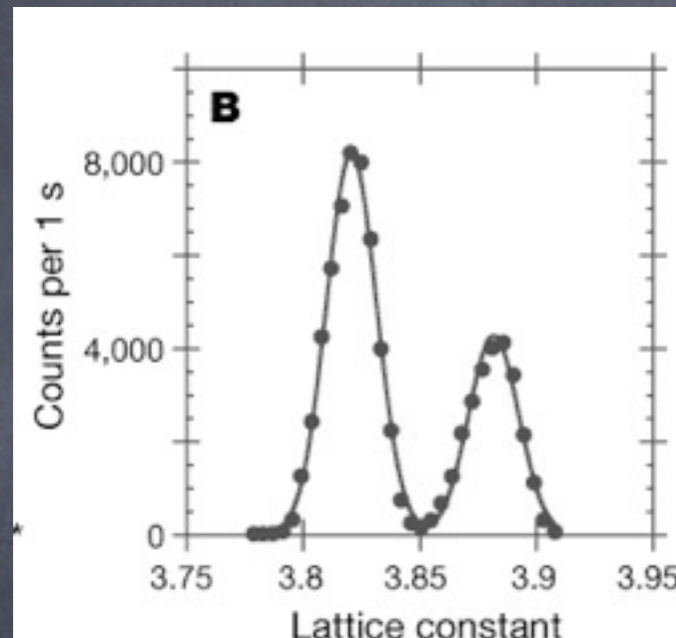
- Resistivity anisotropies as large as factor of 2 have been observed in detwinned single crystals.
- More recently neutron scattering study of magnetic structure of $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ revealed order one anisotropy below well-defined ordering $T \sim 150\text{K}$. [2008 Science 319 597-600]
- More subtle investigations of orientational symmetry breaking can be undertaken by studying the transport in a magnetic field

Cuprate high T_c superconductors experiment facts: Transport anisotropies



- A magnetic field perpendicular to the CuO_2 planes in order to break fourfold symmetry of crystal structure. $\text{La}_{2-x-y}\text{Nd}_y\text{Sr}_x\text{CuO}_4$
- σ_{xx} keeps large value even at the lowest T , reduction of σ_{xy} demonstrates that charge order suppresses transverse motion of carriers.
- Remarkable anisotropy of resistivity tensor was also observed by an in-plane magnetic field in $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$. $x=0.32$ and 0.3
- Results were interpreted as evidence for nematic stripe order. HOWEVER, alternative explanations of anisotropy associated with spin-orbit coupling in antiferromagnetic phase.

Cuprate high Tc superconductors experiment facts: Anisotropic diffraction patterns



- Microscopic approach, directly measure the order parameter. $Q_{\mathbf{k}} \equiv \frac{S(\mathbf{k}) - S(\mathcal{R}[\mathbf{k}])}{S(\mathbf{k}) + S(\mathcal{R}[\mathbf{k}])}$,
- Well-developed structure was observed in inelastic spectrum at vector $\mathbf{Q}_s \sim (0.5+0.1, 0.5)$ and $\mathbf{Q}'_s \sim (0.5, 0.5+0.1)$. Associated with ordering vectors perpendicular to the chain direction. Order parameter $\psi \sim 1$. (left-YBCO)
- Two barely resolved incommensurate peaks at the stripe-order wave vector was observed. However a single sharp peak at chain direction.(right-YBCO)

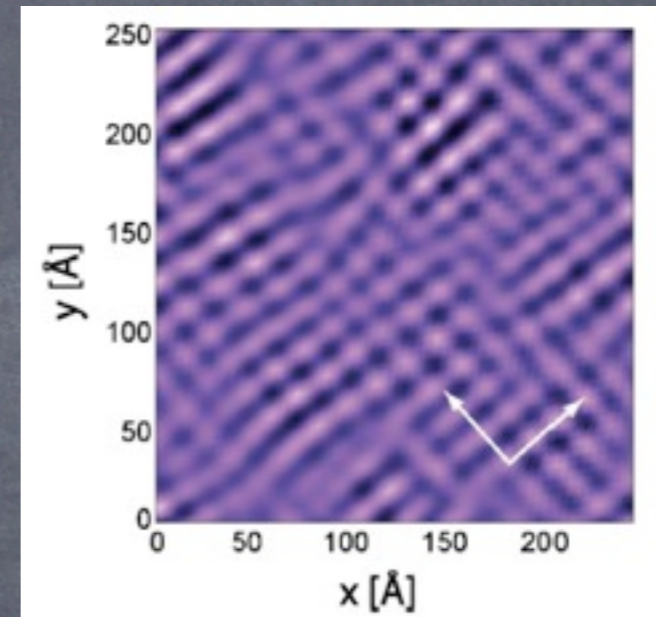
Cuprate high T_c superconductors experiment facts: STM imaging of nematic order

- Because STM is a local but spatially resolved probe, it is actually the optimal probe of nematic order.

- A filtered version of the local-density-of-states map $N_f(\mathbf{r}, E)$ of $\text{Bi}_2\text{Sr}_2\text{CaCu}_2\text{O}_{8+\delta}$, by

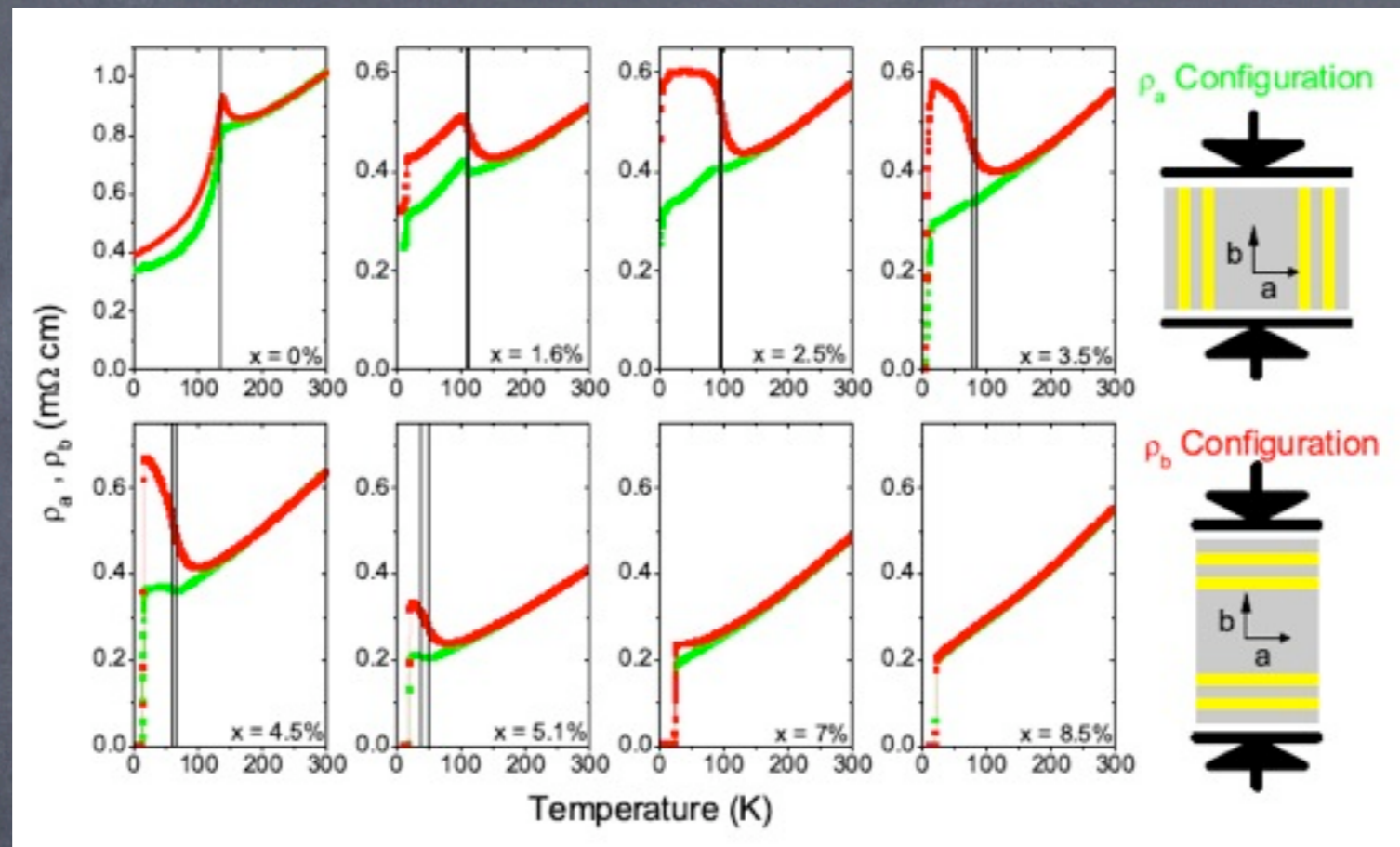
$$N_f(\mathbf{r}, E) = \int d\mathbf{r}' f(\mathbf{r} - \mathbf{r}') N(\mathbf{r}', E),$$

$$f(\mathbf{r}) \propto \Lambda^2 e^{-r^2 \Lambda^2 / 2} [\cos(\pi x / 2a) + \cos(\pi y / 2a)].$$



- The filtered image shows only the portion associated with pinned stripes.
- This particular method of analysis builds directly on: the nematic as a melted stripe-ordered state.

Iron-pnictide high T_c superconductors experiment briefing



- Pressure serves as a symmetry-breaking field.
- Quantitative theory is desperately needed concerns the relation between transport properties and nematic order.

Conclusion and Prospect

- A relative clear picture of nematic state mechanism as melted stripe order. Although microscopic mechanism of stripe order is not clear.
- Nematic detection: macroscopic isotropic → unreasonably large, and strongly T-dependent, anisotropy in electronic response to a small symmetry-breaking field.
- Accumulated experiments facts help us to build insights and intuition.
- It appears structural distortion is a consequence of electron nematicity, maybe important related to iron-pnictide sc.